



DSSSB TGT

PART (A+B)



MATHS

NUMBER THEORY (GRADUATION LEVEL)



09/07/2024 04:30PM



FERMAT'S THEOREM

Fermat's Theorem

If p is a prime number and a denotes an integer such that $(a, p) = 1$, then

$$(8^2, 3) = 1 \pmod{3}$$

$$8^{3-1}, p = 1 \pmod{3}$$

$$\frac{64}{3}, R=1$$

$$a^{p-1} \equiv 1 \pmod{p}$$

$$\text{Co-prime} \left[\frac{a^{(p-1)}}{p} = 1 \text{ (शेषफल)} \right]$$

$$\begin{aligned} a, p &= 1 \\ \text{GCD (HCF)} \\ &\Rightarrow 1 \end{aligned}$$

Theorem: If p is a prime number and a_i denotes an integer, then

$$(a_1 + a_2 + a_3 + a_4 + \cdots + a_n)^p = a_1^p + a_2^p + a_3^p + a_4^p + \cdots + a_n^p + \underline{\underline{M(p)}}$$

where $M(p)$ denotes multiple of p .

$$(2+3)^2 = 25$$

$$2^2 + 3^2$$

$$\Rightarrow 4 + 9 = 13 + 2(6)$$

$$L^x | x^1$$

1. If $(n, 17) = 1$ where k is any positive integer then $n^{16k} - 1$ is divisible by

a. 18

b. 17

c. 15

d. 20

$$\begin{array}{r} 17 \overline{) n^{16k}} \quad \left[a \right. \\ \underline{1} \\ 1 \end{array}$$

$$n^{16k} = 17a + 1$$

$$\underline{n^{16k} - 1 = 17a} \quad (n^{16k} - 1) = (\text{mod } 17)$$

$$(a, p) = 1$$

$$a^{p-1} = 1 \pmod{p}$$

$$n^{16} = 1 \pmod{17}$$

$$(n^{16})^k = 1^k \pmod{17}$$

$$n^{16k} = 1 \pmod{17}$$

$$n^{16k} - 1 = ?$$

$$\begin{array}{r} 17 \overline{) 18} \quad (1) \\ \underline{17} \\ 1 \end{array}$$

$$18 - 1 = 17$$

$$(4, 17) \rightarrow \text{HCF} = 1$$

$$17 \rightarrow \text{Prime}$$

$$\frac{a^{p-1}}{p} = R=1$$

 \Rightarrow

$$\frac{4^{18}}{17}$$

$$, R=?$$

$$\frac{4^{16}}{17} = R=1$$

$$\Rightarrow \frac{4^{16} \times 4^2}{17} =$$

$$\frac{1 \times 16}{17} \Rightarrow R=16$$

$$17-1=16$$

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$$\left[\frac{a^{p-1}}{p}, R=1 \right]$$

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$$\frac{17^{18} \times 17^{18} \times 17^{18} \times 17^{18}}{19}$$

$$\Rightarrow \frac{17^{182}}{19}, R=? \Rightarrow \frac{(17^{18})^{10} \times 17^2}{19}$$

$$\Rightarrow \frac{289}{19} \quad R=4$$

$$\begin{array}{ccc}
 \frac{2^2}{3} & \frac{(2^2)^4}{3} & \Rightarrow \frac{2^2 \times 2^2 \times 2^2 \times 2^2}{3} \\
 R=1 & R=1 & \Rightarrow \frac{256}{3} \Rightarrow \textcircled{1}
 \end{array}$$

TOPIC - NUMBER THEORY

1. Divisibility (Theorems On Divisibility,

HCF → G.C.D. & L.C.M.)

2. Possible Solutions or Integer Solutions

3. Relatively prime Number

4. Congruences

5. Residue System (mod m)

6. Chinese Remainder Theorem

7. Euler's ϕ Function

→ 8. Fermat's Theorems

9. Euler's Theorems

Divisibility →

Osculator (एकाधिक)



- ✓ **10. Wilson's Theorems**
- ✓ **11. Some Functions of Number Theory**
- ✓ **12. Positive Divisors →**
- ✓ **13. Number of Divisors → No of factors**
- ✓ **14. Sum of divisors → sum of factors**