

# Plane geometry

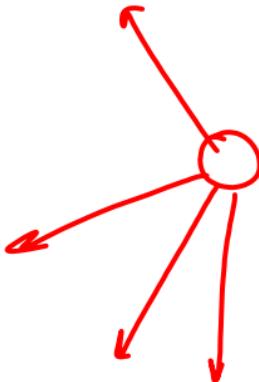
- 1. lines & angles
- 2. Triangles
- 3. Quadrilaterals
- 4. Polygons
- 5. Circles
- 6. Misc. theorems

# Lines & Angles

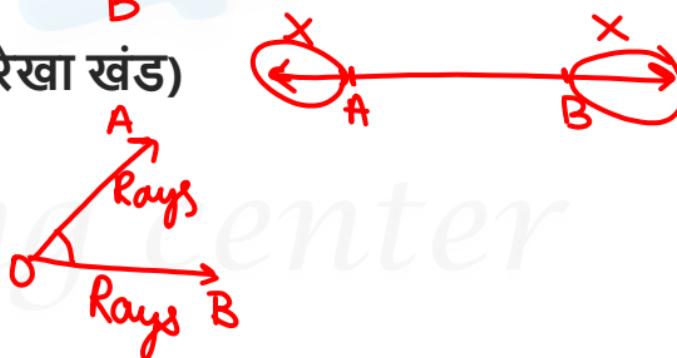
(रेखा एवं कोण)

*coaching center*

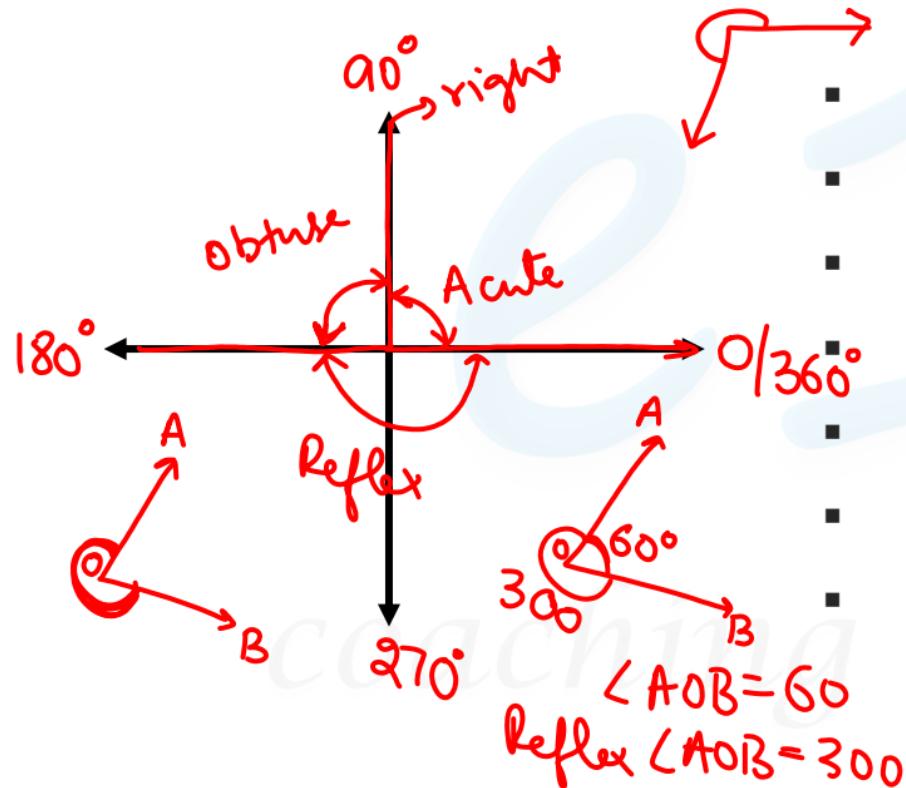
# Basic terminology:



- **Point (बिंदु)** • | a circle with zero radius/a dimension less figure  
विमाहीन
- **Line (रेखा)**  $\longleftrightarrow$  1D
- **Plane (समतल)**  2D
- **Ray (किरण)**  $\xrightarrow{A \rightarrow B}$
- **Line segment (रेखा खंड)**
- **Angle (कोण)**  $\overset{\text{part}}{\text{Angle}}$

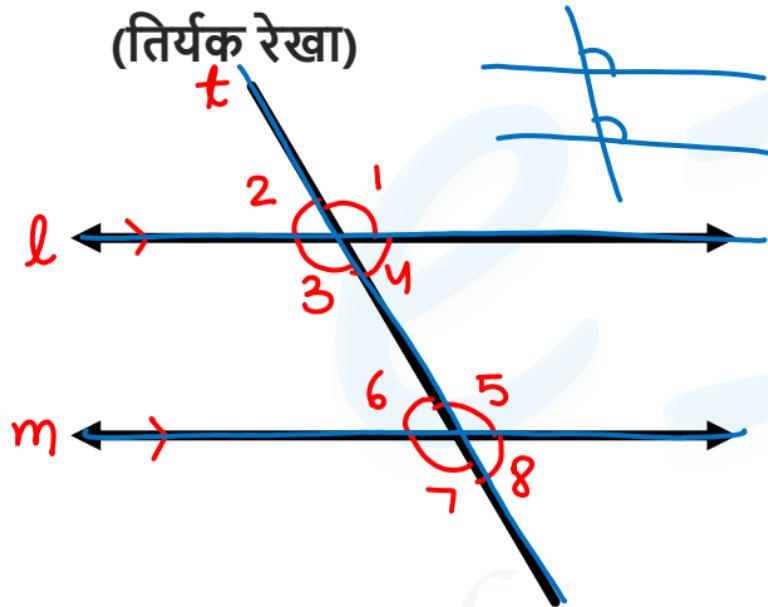


# Types of angles (कोणों के प्रकार):



- **Zero Angle (शून्य कोण)**  $0^\circ$
- **Acute Angle (न्यून कोण)**  $0 < \theta < 90^\circ$
- **Right Angle (सम कोण)**  $= 90^\circ$
- **Obtuse Angle (अधिक कोण)**  $90 < \theta < 180^\circ$
- **Straight angle (सरल / ऋजु कोण)**  $= 180^\circ$
- **Reflex angle (वृहत कोण)**
- **Complete angle (पूर्ण कोण)**

# Angles in parallel lines (समानांतर रेखाओं में कोण):

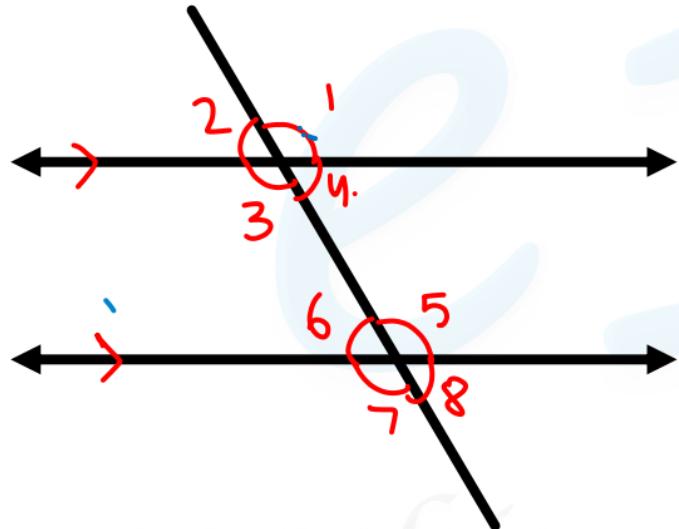


Corresponding angles:  
संगत कोण

$\angle 1 \text{ & } \angle 5$   
 $\angle 2 \text{ & } \angle 6$   
 $\angle 3 \text{ & } \angle 7$   
 $\angle 4 \text{ & } \angle 8$

If lines are || then C.A's are equal & Vice-versa

# Angles in parallel lines (समानांतर रेखाओं में कोण):



Alternate angles:  
एकांतर कोण

Interior (अंतः) ( $\angle 3, \angle 4, \angle 5, \angle 6$ )

Alt Int L's

$\angle 4 \& \angle 6$   
 $\angle 3 \& \angle 5$

} equal

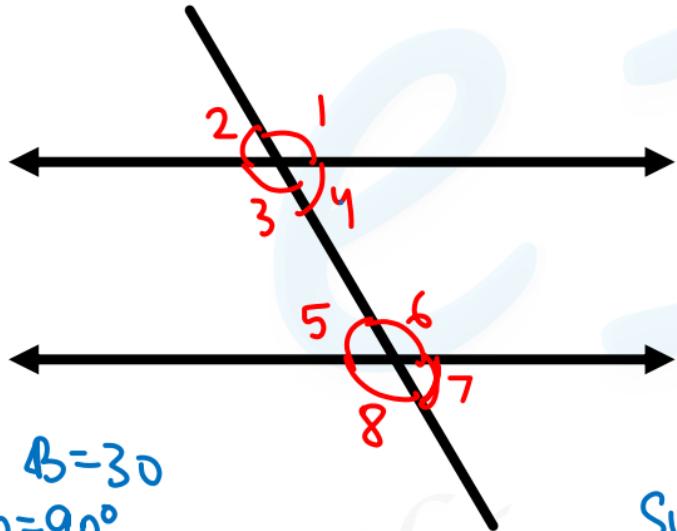
Exterior (बाह्य) ( $\angle 1, \angle 2, \angle 7, \angle 8$ )

Alt Ext L's

$\angle 1 \& \angle 7$   
 $\angle 2 \& \angle 8$

} equal

# Angles in parallel lines (समानांतर रेखाओं में कोण):



$$A = 60 \quad B = 30 \\ \text{Sum} = 90^\circ$$

Complementary  
पूरक / कोटि पूरक

## Angles on same side:

Interior (अंतः) on the same side

$\angle 4 \& \angle 6$  } Supplementary  
 $\angle 3 \& \angle 5$  } Supplementary

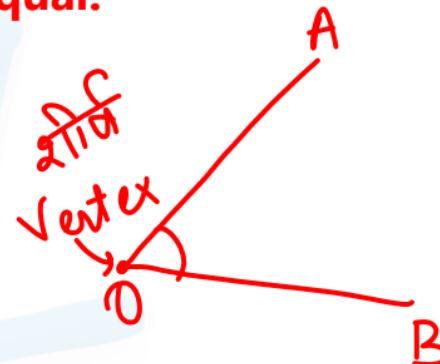
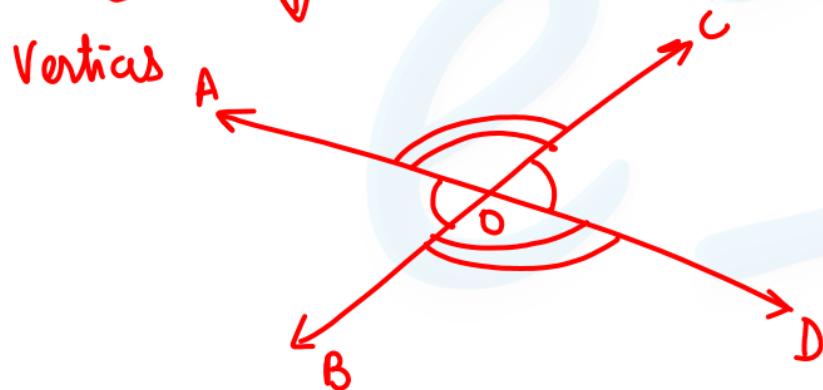
Exterior (बाह्य) on the same side

$\angle 1 \& \angle 7$  } संपूरक  
 $\angle 2 \& \angle 8$  } संपूरक

Supplementary  
सम्पूरक

## Some basic points:

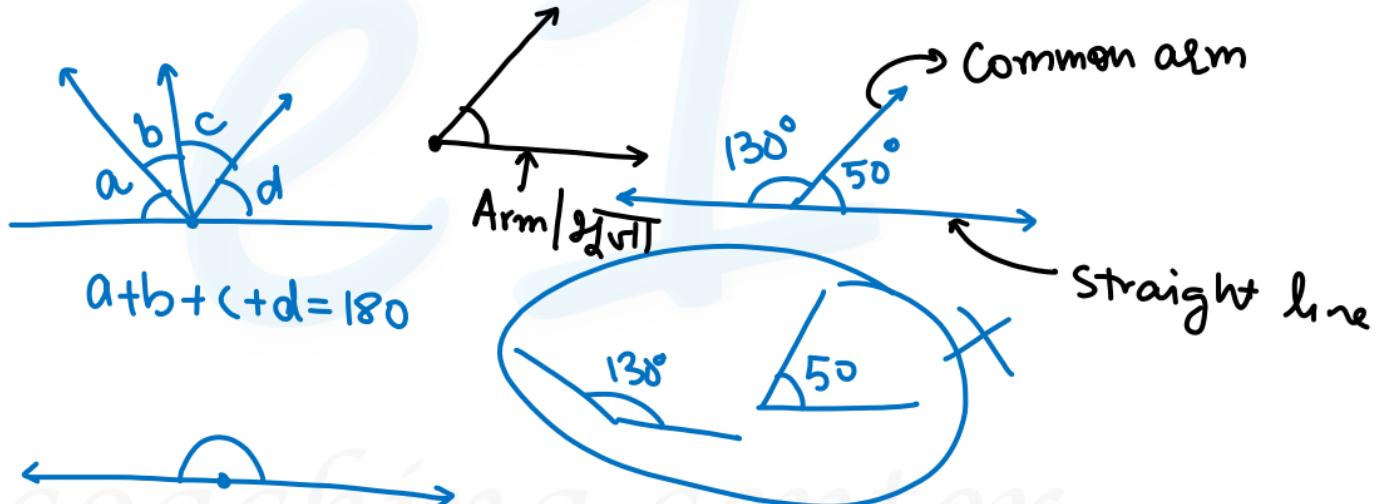
- **Vertically opposite angles are equal.**  
**(शीर्षभिमुख कोण बराबर होते हैं)**



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## Some basic points:

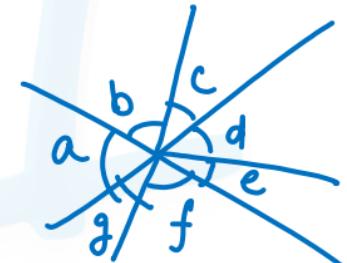
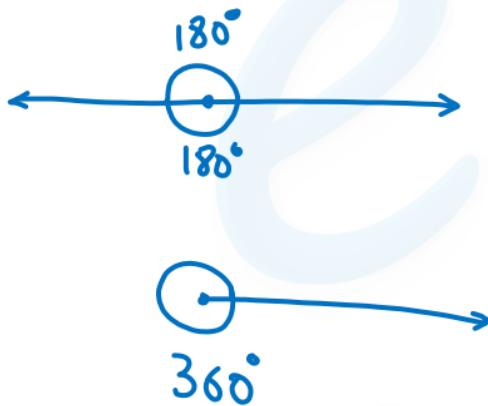
- **Sum of angles on a line is  $180^\circ$ . (Linear pair)** *two L's*  
**(एक रेखा पर बने कोणों का योग  $180^\circ$  होता है), (रेखिक युग्म)**



## Some basic points:

- **Sum of angles around a point is  $360^\circ$ .**

(एक बिंदु के बाहर बने सभी कोणों का  $360^\circ$  योग होता है)

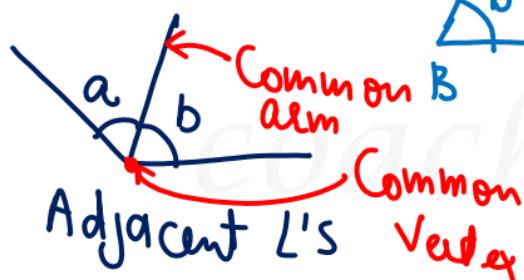
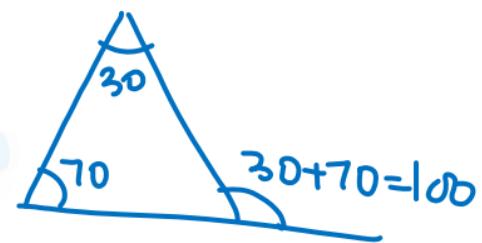
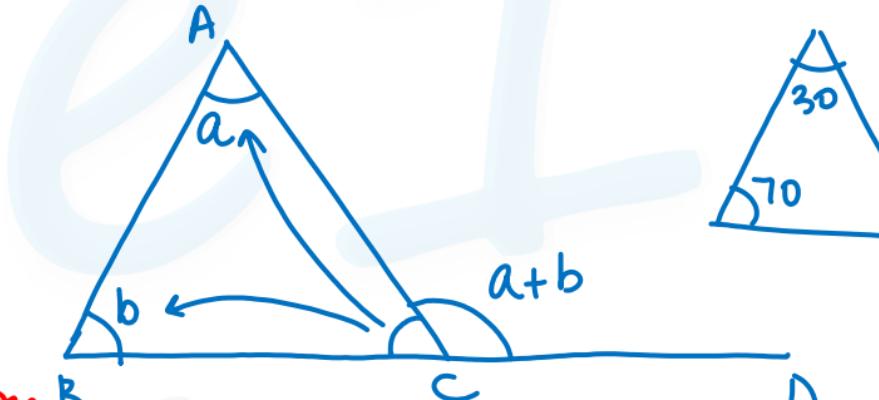
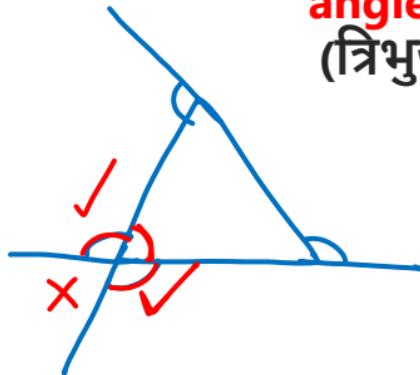


$$a+b+c+d+e+f+g = 360^\circ$$

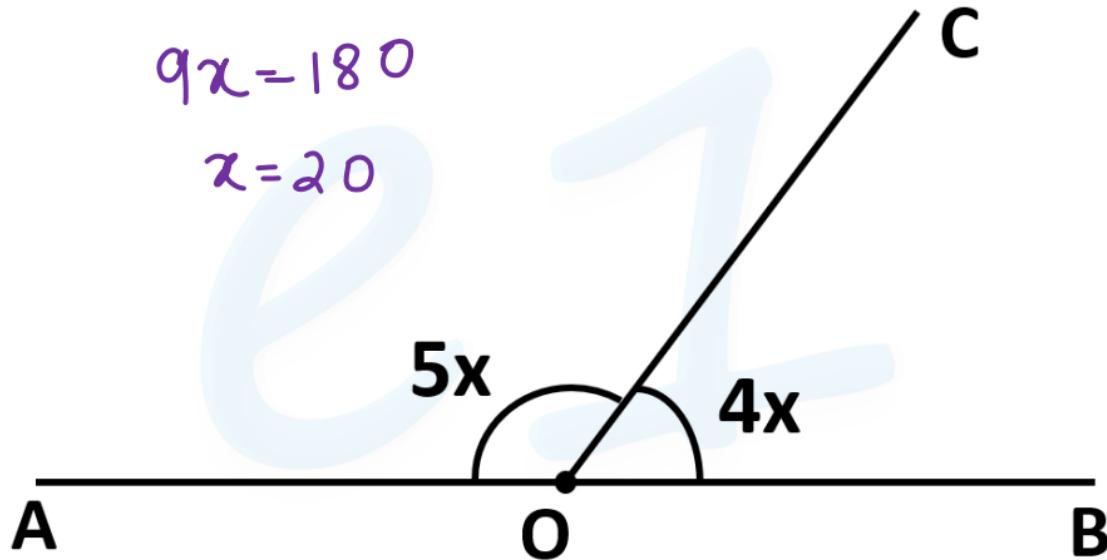
## Some basic points:

- Exterior angle of a triangle is equal to sum of interior opposite angles.

(त्रिभुज का बाह्य कोण अंतःअभिमुख कोणों के योग के बराबर होता है)



1. Find  $x$ .

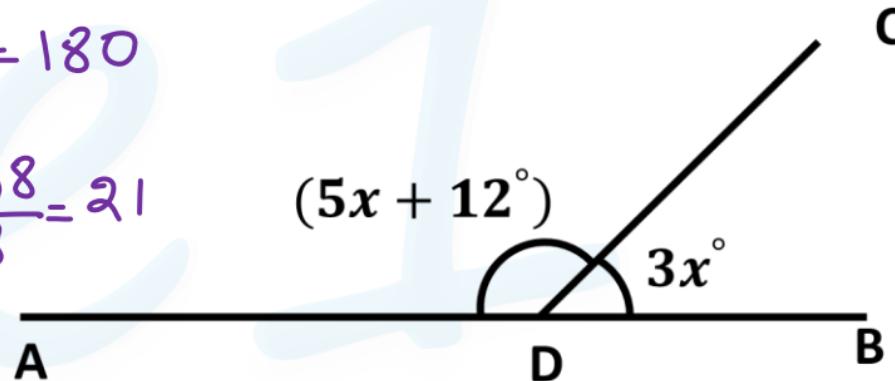


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2. Find  $x$ .

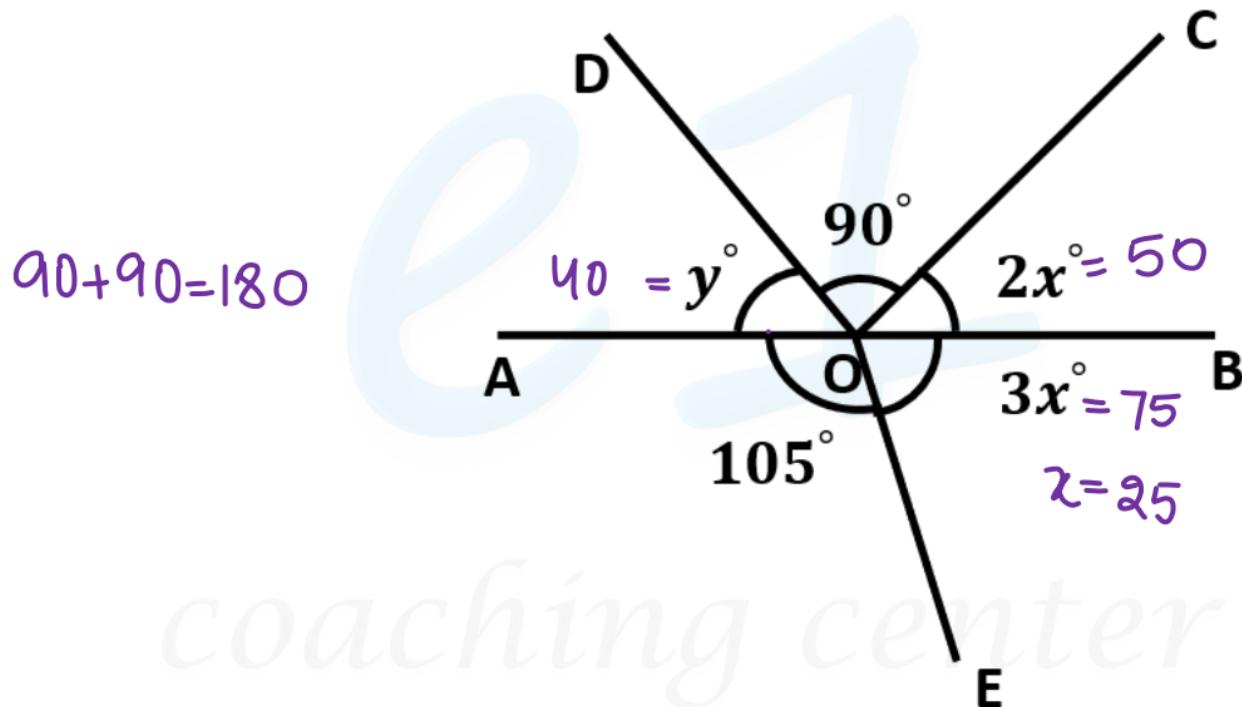
$$8x + 12 = 180$$

$$x = \frac{168}{8} = 21$$



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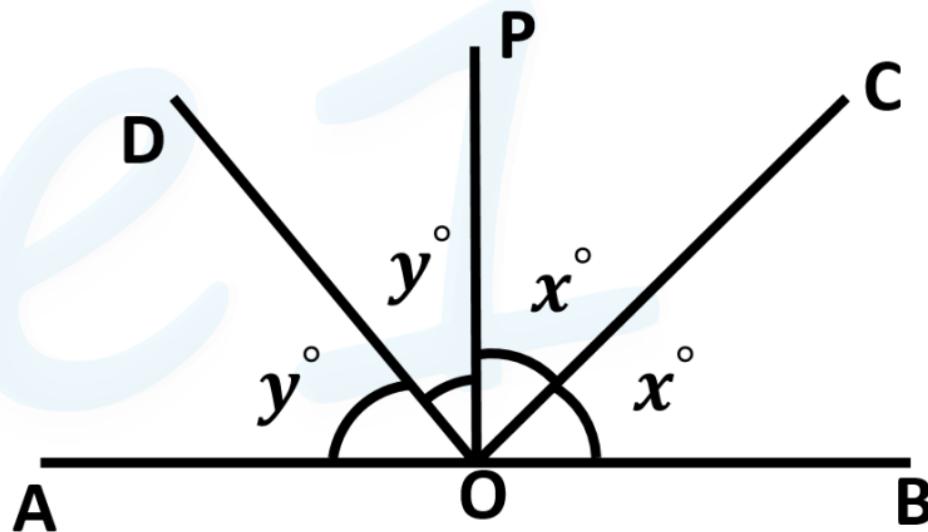
3. Find y. AOB is a straight line



4. Find  $\angle COD = 90$

AOB straight line

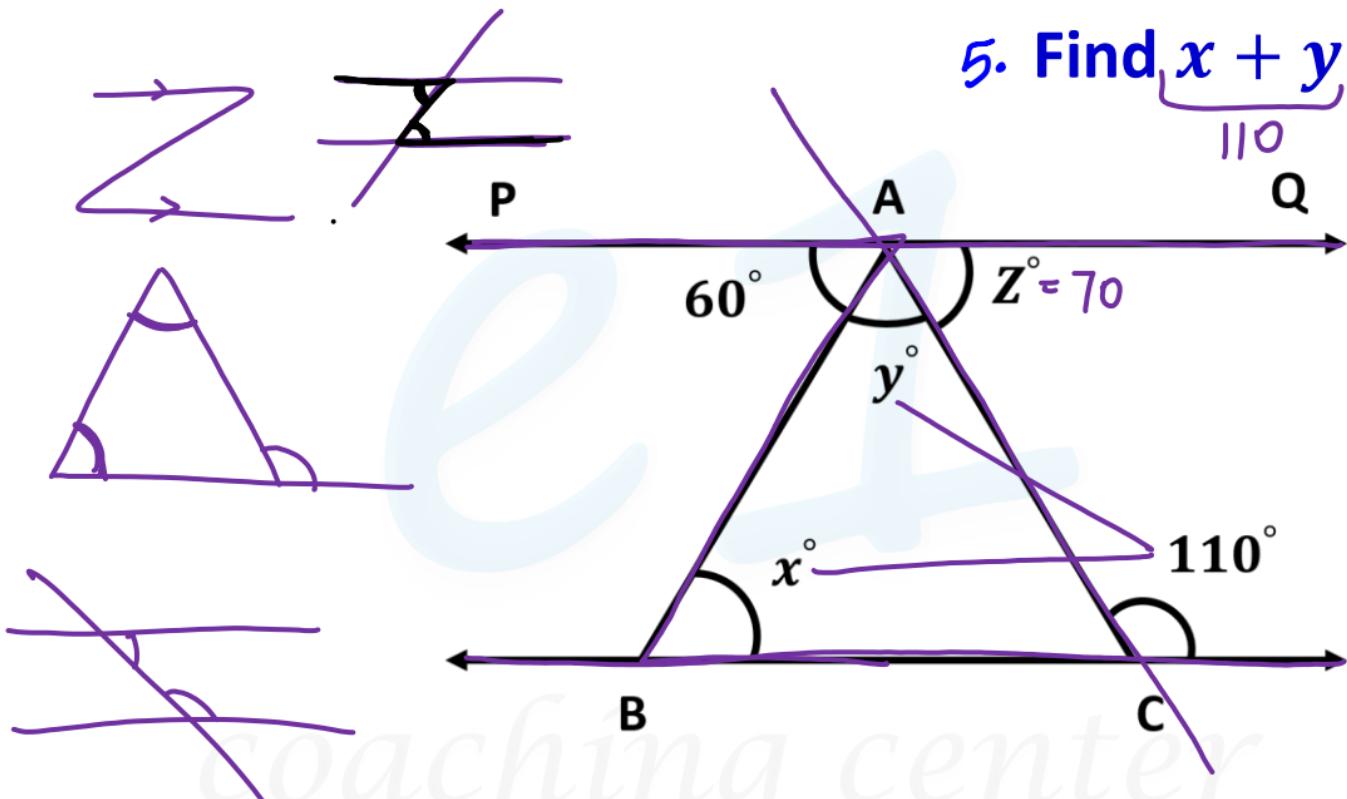
$$\angle x + \angle y = 180^\circ$$



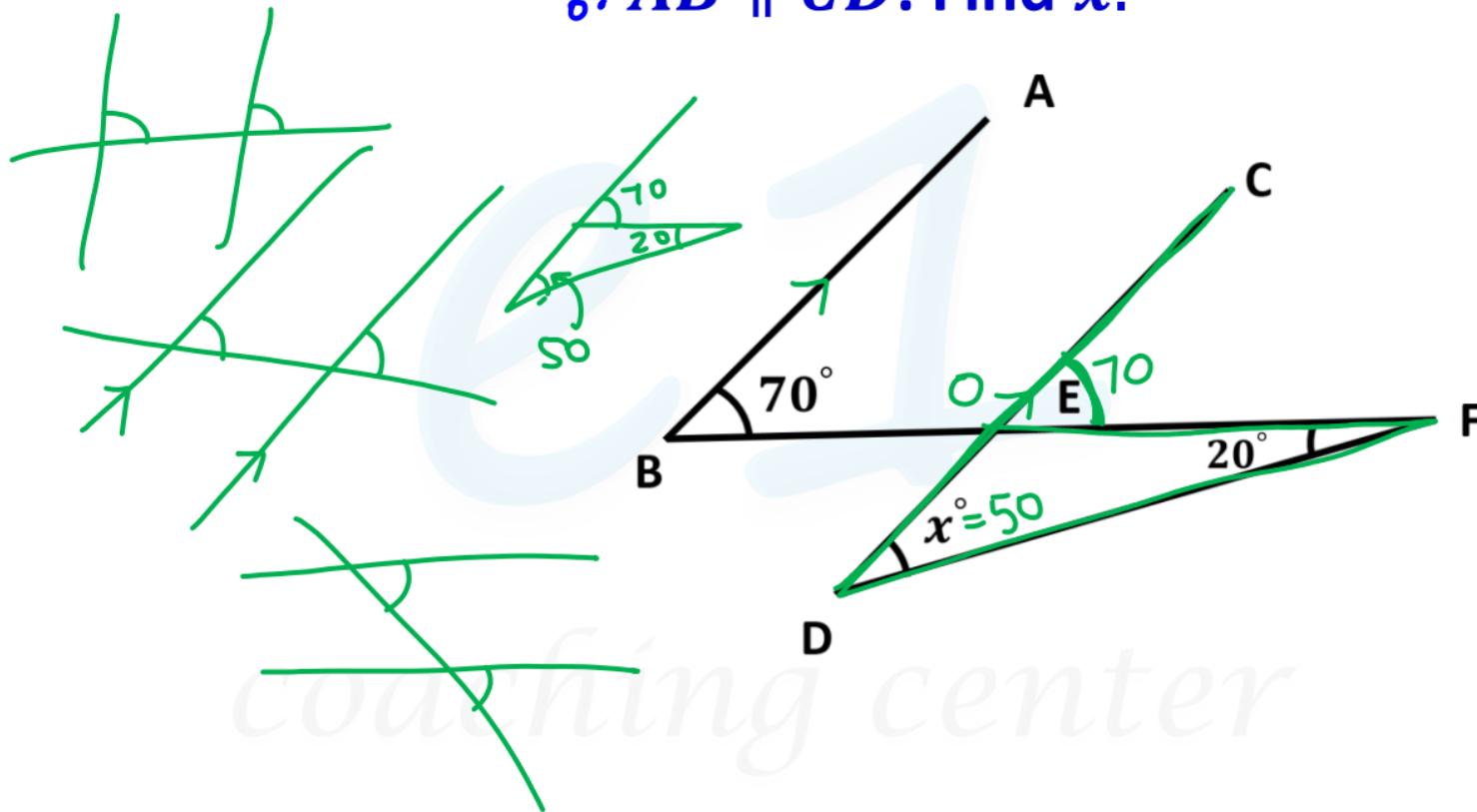
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5. Find  $x + y - z = 40$

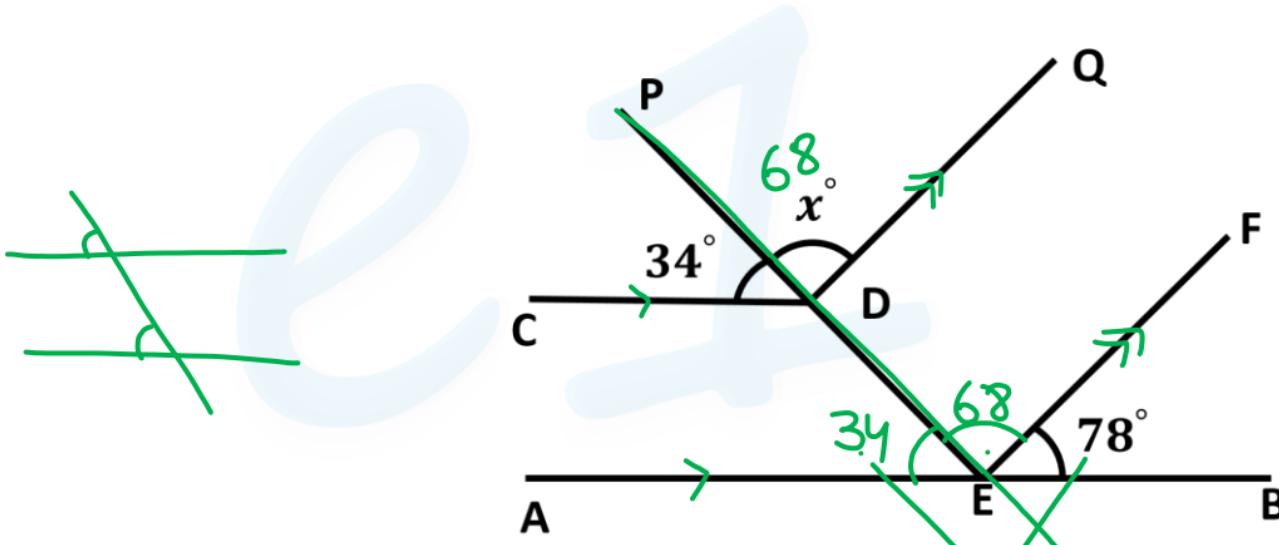
$$\begin{array}{c} \boxed{x} \\ \boxed{y} \\ \hline \boxed{z} \end{array}$$
$$\begin{array}{c} 110 \\ \hline 70 \end{array}$$



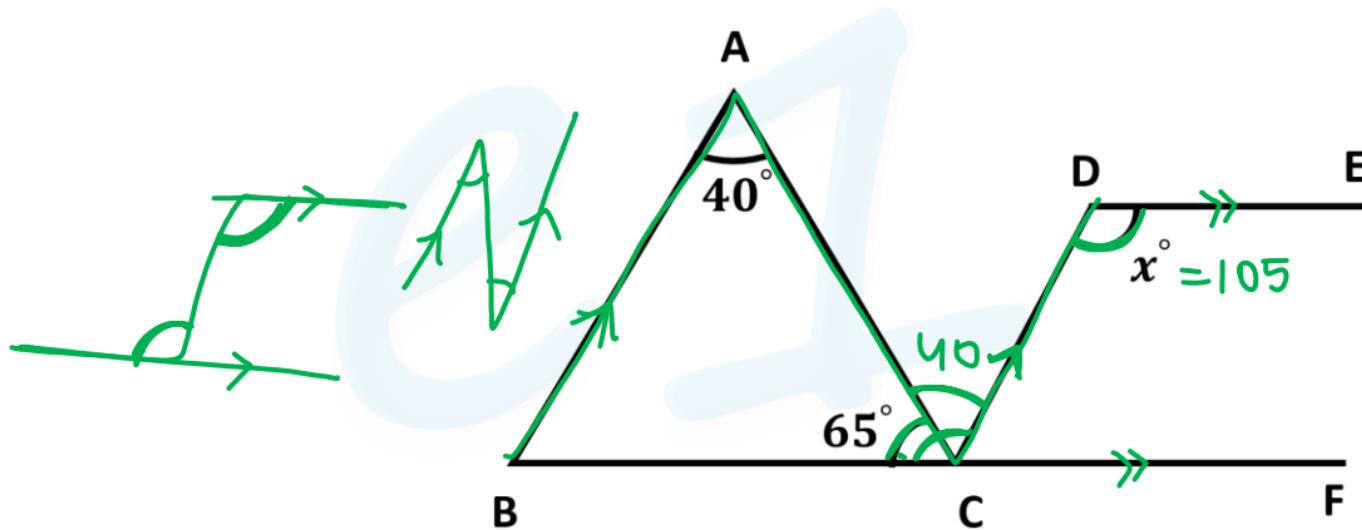
6.  $AB \parallel CD$ . Find  $x$ .



7.  $AB \parallel CD$  and  $EF \parallel DQ$ . Find  $x$ .

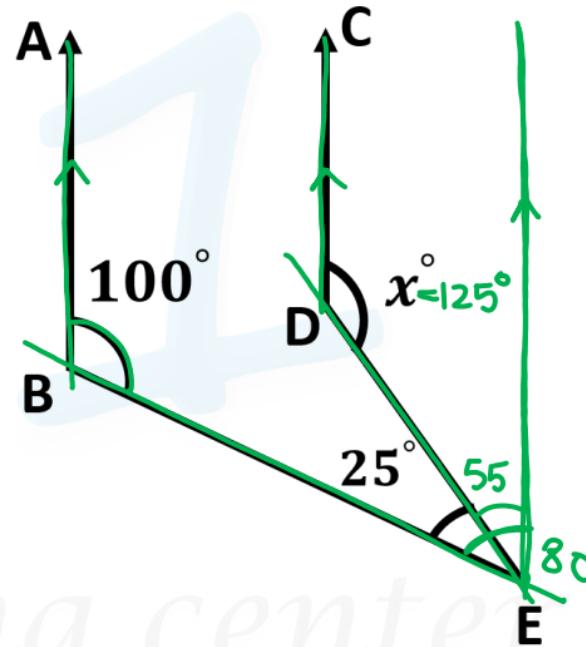
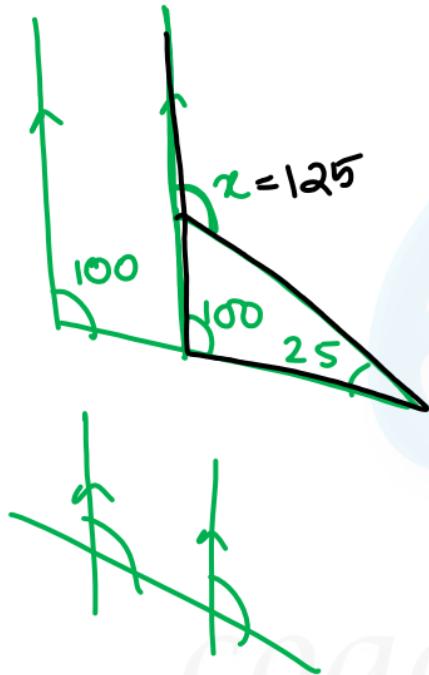


8.  $AB \parallel DC$  and  $DE \parallel BF$ . Find  $x$ .

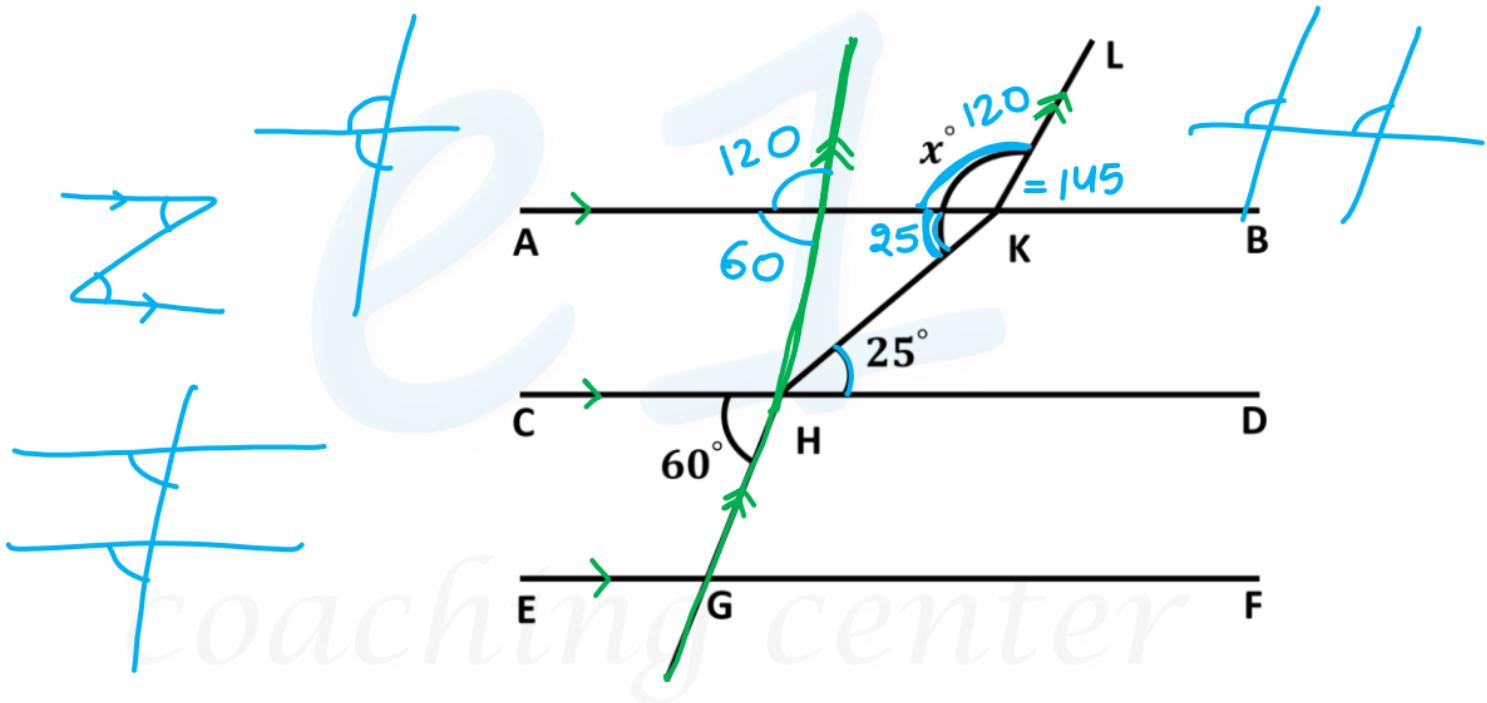


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q.  $AB \parallel CD$ . Find  $x$ .



Q.  $AB \parallel CD \parallel EF$  and  $GH \parallel KL$ . Find  $x$ .



11. In the figure given above,  $AB$  is parallel to  $CD$ . If  $\angle DCE = x$  and  $\angle ABE = y$ , then what is  $\angle CEB$  equal to?

निम्न दी गई आकृति में  $AB$ ,  $CD$  के समान्तर हैं। अगर  $\angle DCE = x$  और  $\angle ABE = y$  हैं तो  $\angle CEB = ?$

a)  $y - x$

b)  $\frac{x+y}{2}$

c)  $x + y - \left(\frac{\pi}{2}\right)$

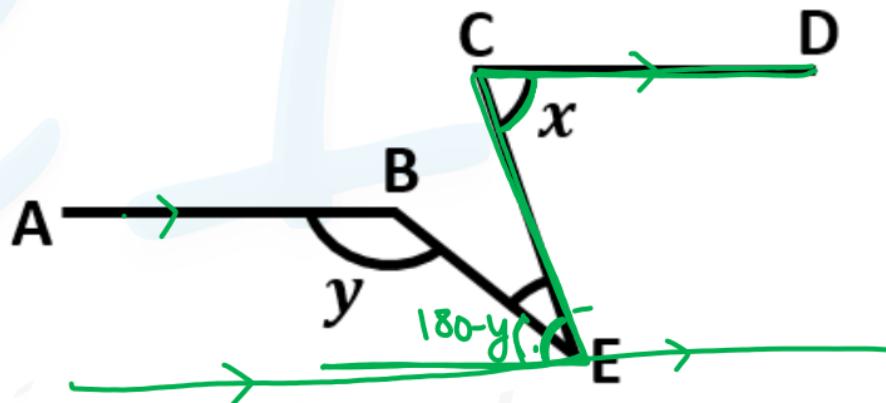
d)  $x + y - \pi$

$\chi = 180 - y + \angle CEB$

$$\chi - 180 + y$$

$$= x + y - 180$$

$$180^\circ = \pi^c$$



12. Three straight lines X, Y and Z are parallel and the angles are as shown in the figure above. What is  $\angle AFB$  equal to:

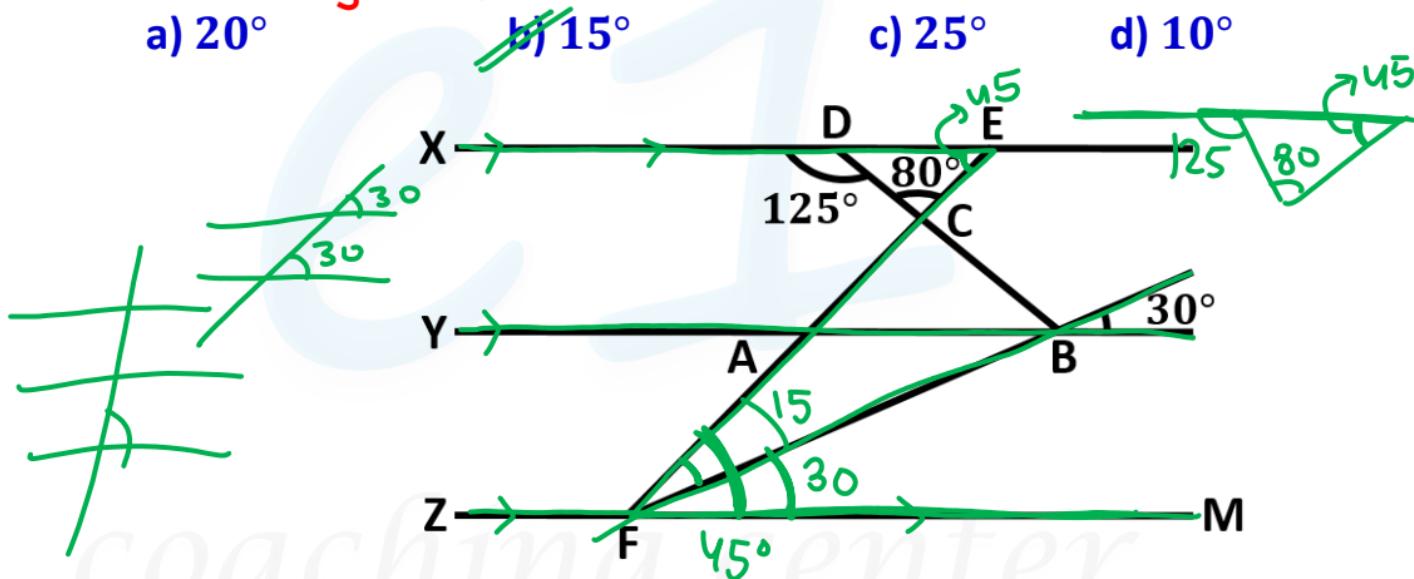
तीन सीधी रेखाएं X, Y और Z समान्तर हैं और सभी कोण आकृति में दिए गए के अनुसार हैं।  $\angle AFB = ?$

- a)  $20^\circ$

- b)  $15^\circ$

- c)  $25^\circ$

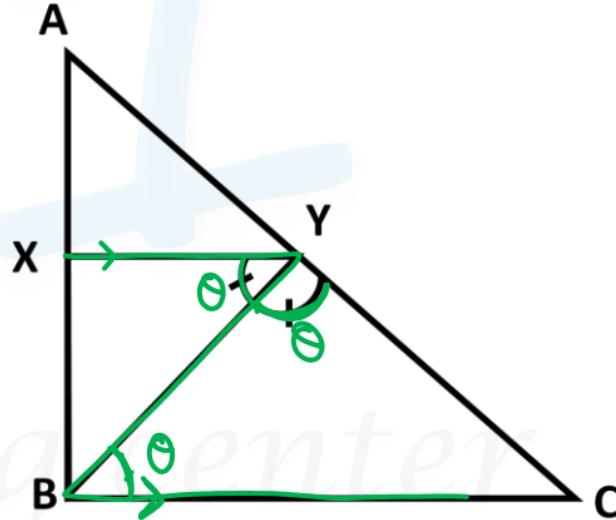
- d)  $10^\circ$

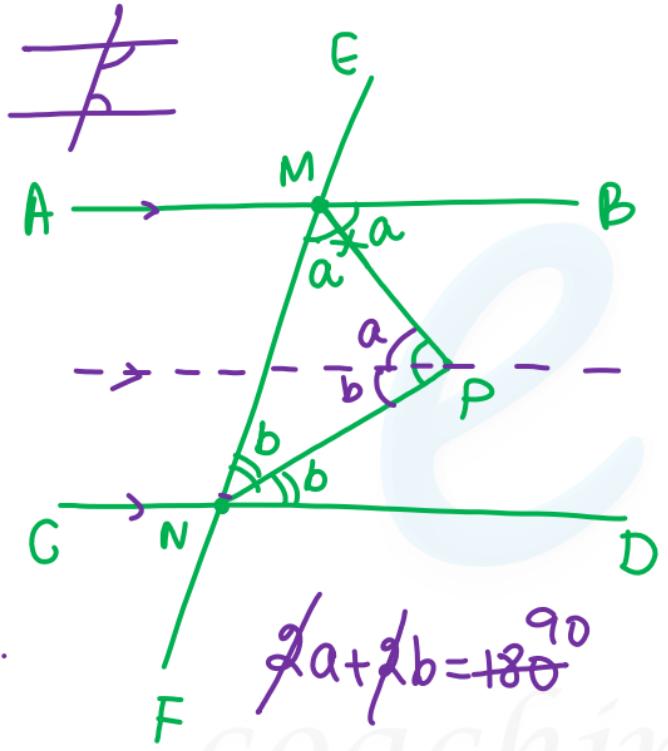


13. In a  $\triangle ABC$ , a line XY parallel to BC intersects AB at X and AC at Y. If BY bisects angle XYC, then  $m \angle CBY : m \angle CYB$  is:

एक त्रिभुज  $\triangle ABC$  में, रेखा XY रेखा BC के समानांतर है तथा रेखा BY कोण XYC को द्विभाजित करती है, तो  $m \angle CBY : m \angle CYB$  बताओ।

- a) 5 : 4      b) 4 : 5      c) 1 : 1      d) 6 : 5





14. Two parallel lines AB and CD are intersected by a transversal EF at M and N respectively. The lines MP and NP are the bisectors of interior angles  $\angle BMN$  and  $\angle DNM$  on the same side of the transversal. Then  $\angle MPN$  is equal to :

AB और CD, दो समानांतर रेखाएं एक EF नामक प्रतिष्ठेदी द्वारा M और N पर कटी गयी। MP और NP रेखाएं कोण BMN और कोण DNM को द्विभाजित करती हैं। तो कोण MPN का मान बताओ।

- a)  $60^\circ$
- b)  $90^\circ$
- c)  $45^\circ$
- d)  $120^\circ$