

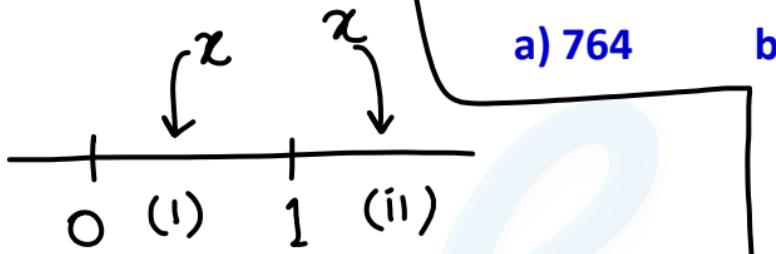
226. If $x > 1$ and $x^2 + \frac{1}{x^2} = 83$ then $x^3 - \frac{1}{x^3} = ?$
 अगर $x > 1$ और $x^2 + \frac{1}{x^2} = 83$ है तो $x^3 - \frac{1}{x^3} = ?$

a) 764

b) 750

c) ~~756~~
~~-2~~

d) 760



$$(i) x = \frac{1}{2}, \frac{1}{3}, \frac{1}{4}$$

$$\frac{1}{x} = 2, 3, 4$$

$$x < \frac{1}{x}$$

$$x^2 < \frac{1}{x^2}$$

$$(ii) x = 2, 3, 4$$

$$\frac{1}{x} = \frac{1}{2}, \frac{1}{3}, \frac{1}{4}$$

$$x > \frac{1}{x} \quad x - \frac{1}{x} > 0$$

$$x - \frac{1}{x} = -ve$$

$$x^2 - \frac{1}{x^2} = -ve$$

$$\left(x - \frac{1}{x} \right)^2 = 81$$

$$x - \frac{1}{x} = \pm 9 \quad x = 9$$

$$\begin{array}{r} 729 \\ + 27 \\ \hline 756 \end{array}$$

227. If $x^4 + \frac{1}{x^4} = 119$, and $x > 1$, then the value of $x^3 + \frac{1}{x^3} = ?$

अगर $x^4 + \frac{1}{x^4} = 119$, और $x > 1$ है तो $x^3 + \frac{1}{x^3} = ?$

a) 36

b) $16\sqrt{13}$

c) 18

~~d) $10\sqrt{13}$~~

$$(x^2)^2 + \left(\frac{1}{x^2}\right)^2 + 2x^2 \cancel{- \frac{1}{x^2}}$$

$$13\sqrt{3} - 3\sqrt{3}$$

$$\left(x^2 + \frac{1}{x^2}\right) = \sqrt{121} = 11$$

$$x^2 + \frac{1}{x^2} = \sqrt{13}$$

228. If $m^4 + \frac{1}{m^4} = 119$, then $m - \frac{1}{m} = ?$

अगर $m^4 + \frac{1}{m^4} = 119$ है तो $m - \frac{1}{m} = ?$

- ~~a) ± 3~~ $+2$ b) 4 $+2$ c) ± 2 d) ± 1

$$m^2 + \frac{1}{m^2} = 11 - 2$$

$$m - \frac{1}{m} = \pm 3$$

coaching center

229. If $x^4 + \frac{1}{x^4} = 322$, then what is the value of $x^3 - \frac{1}{x^3}$?

यदि $x^4 + \frac{1}{x^4} = 322$ है, तो $x^3 - \frac{1}{x^3}$ का मान क्या है?

- a) 16 b) 96 c) 76 d) 46

$$x^2 + \frac{1}{x^2} = 18$$

$$-2 \quad -2$$

$$64 + 12$$

$$x - \frac{1}{x} = 4$$

coaching center

230. If $x^8 - 1442x^4 + 1 = 0$, then a possible value of $x - \frac{1}{x}$ is:

यदि $x^8 - 1442x^4 + 1 = 0$, तो $x - \frac{1}{x}$ का संभावित मान है:

a) 5

b) 8

c) 4

d) 6

$50n \pm 12$

$\boxed{1444}$

= 38

$$x^4 + \frac{1}{x^4} = 1442$$

+2
+2

$$x^2 + \frac{1}{x^2} = 38^{-2}$$

$$x - \frac{1}{x} = \pm 6$$

$50n \pm 12$ Q3). If $x^4 + \frac{1}{x^4} = 3842$, then the positive value of $x + \frac{1}{x}$ will be:

यदि $x^4 + \frac{1}{x^4} = 3842$ है, तो $x + \frac{1}{x}$ का धनात्मक मान ज्ञात करें।

- a) 12 +2 ~~b) 8~~ +2 c) 10 d) 6

$$\sqrt{\overline{3844}}$$

↓
6 -

$$x^2 + \frac{1}{x^2} = 62^2$$

$$x + \frac{1}{x} = 8$$

232. If $x > 0$ and $x^4 + \frac{1}{x^4} = 2207$, What is the value of

$$(x^5 + \frac{1}{x^5})?$$

यदि $x > 0$ और $x^4 + \frac{1}{x^4} = 2207$ है, तो $(x^5 + \frac{1}{x^5})$
का मान क्या होगा?

- a) 15141 b) 15134 c) 15130 d) 15127

$$\begin{array}{r} 2209 \\ \hline 47 \\ \downarrow \\ 47 \end{array}$$

$$x^2 + \frac{1}{x^2} = 47^{+2}$$

$$x + \frac{1}{x} = 7$$

$$\begin{array}{r} 343 \\ - 21 \\ \hline 322 \end{array}$$

$$\left(x^3 + \frac{1}{x^3} \right) \left(x^2 + \frac{1}{x^2} \right) - \left(x + \frac{1}{x} \right)$$

$$= 332 \times 47 - 7$$

Unit digit = 7

233. If $x^4 + \frac{1}{x^4} = 6887$, then the positive value of $x - \frac{1}{x}$ is:

यदि $x^4 + \frac{1}{x^4} = 6887$ है, तो $x - \frac{1}{x}$ का घनात्मक मान ज्ञात करें।
a) 12 b) 9 c) 15 d) 8

$$x^2 + \frac{1}{x^2} = 83$$

$$-2$$

$$x - \frac{1}{x} = 9$$

$$\begin{array}{r} 6887 \\ \hline 83 \end{array}$$

± 17
 $100 - 17$

coaching center

234. If $x^4 + \frac{1}{x^4} = 14159$, Then a Possible Value of $x + \frac{1}{x}$ is:

यदि $x^4 + \frac{1}{x^4} = 14159$ है, तो $x + \frac{1}{x}$ का संभव मान क्या है?

a) 81 b) 69 c) 11 d) 121

$$x^2 + \frac{1}{x^2} = 119$$

$$x + \frac{1}{x} = 11$$

$$\begin{array}{r} 119 \\ \times 11 \\ \hline 119 \\ 119 \\ \hline 1309 \end{array}$$

coaching center

235. If $x^4 + \frac{1}{x^4} = \frac{257}{16}$ then find $\frac{8}{13}(x^3 + \frac{1}{x^3})$, Where $x > 0$.

यदि $x^4 + \frac{1}{x^4} = \frac{257}{16} + 2$ तो $\frac{8}{13}(x^3 + \frac{1}{x^3})$ ज्ञात कीजिए, जब $x > 0$ है।

- ~~a) 5~~ +2 b) 4 c) 6 d) 8

$$x^2 + \frac{1+2}{x^2} = \sqrt{\frac{257+32}{16}} = \frac{17}{4} + 2$$

$$x + \frac{1}{x} = \sqrt{\frac{25}{4}} = \frac{5}{2}$$

$$\frac{8}{13} \times \frac{65}{8} = 5$$

$$x^3 + \frac{1}{x^3} = \frac{125}{8} - \frac{15 \times 4}{2 \times 4} = \frac{65}{8}$$

236. If $\frac{x^8+1}{x^4} = 14$, then the value of $\frac{x^{12}+1}{x^6}$ is:

यदि $\frac{x^8+1}{x^4} = 14$ है, तो $\frac{x^{12}+1}{x^6}$ का मान क्या है?

- a) 16 b) 14 c) 52 d) 64

$$x^4 + \frac{1+2}{x^4} = 14+2$$

$$x^2 + \frac{1}{x^2} = 4.$$

$$x^6 + \frac{1}{x^6} = 64 - 2 = 52$$

$3x$

coaching center

$$(\sqrt{2})^3 = 2\sqrt{2}$$

$$(\sqrt{5})^3 = 5\sqrt{5}$$

$$\begin{aligned} a^3 + \frac{1}{a^3} &= 2(\sqrt{13}+1) \underbrace{\sqrt{2(\sqrt{13}+1)}} - 3 \underbrace{\sqrt{2(\sqrt{13}+1)}} \\ &= \sqrt{2(\sqrt{13}+1)} \left(2\sqrt{13} + \frac{-3}{\sqrt{13}+1} \right) \end{aligned}$$

$$a^2 + \frac{1}{a^2} = \sqrt{52} = 2\sqrt{13} \quad +2$$

$$a + \frac{1}{a} = \sqrt{2\sqrt{13} + 2} = \sqrt{2(\sqrt{13}+1)}$$

237. If $a^4 + \frac{1}{a^4} = 50, a > 0$, then find the value of $a^3 + \frac{1}{a^3}$

यदि $a^4 + \frac{1}{a^4} = 50, a > 0$, तो

$a^3 + \frac{1}{a^3}$ का मान ज्ञात कीजिए।

a) $\sqrt{2(1 + \sqrt{13})} + (-1 + 2\sqrt{13})$

b) $\sqrt{2(1 - \sqrt{13})} - (-1 + 2\sqrt{13})$

c) $\sqrt{2(1 + \sqrt{13})(-1 - 2\sqrt{13})}$

d) $\sqrt{2(1 + \sqrt{13})(-1 + 2\sqrt{13})}$

coaching center

238. If $a^2 + \frac{1}{(a-3)^2} - 6a = 9$, then $(a-3) - \frac{1}{(a-3)}$?

यदि $a^2 + \frac{1}{(a-3)^2} - 6a = 9$ है तो $(a-3) - \frac{1}{(a-3)}$ का मान होगा :

~~a) 4~~

b) $2\sqrt{5}$

c) 3

d) An Imaginary no.

$$(a^2 - 6a) + \frac{1}{(a-3)^2} = 9 + 9$$

$$(a-3)^2 + \frac{1}{(a-3)^2} = 18 - 2$$

$$(a-3) - \frac{1}{(a-3)} = \sqrt{16} = 4$$

239. If $x^2 + x = 5$, then find the value of $(x+3)^3 + \frac{1}{(x+3)^3}$.

यदि $x^2 + x = 5$ है, तो $(x+3)^3 + \frac{1}{(x+3)^3}$ का मान ज्ञात कीजिये।

- a) 110 b) 140 c) 125 d) 120

$$(x+3) + \frac{1}{(x+3)} = \frac{x^2 + 6x + 9 + 1}{x+3} = \frac{5x + 15}{x+3} = \frac{5(x+3)}{(x+3)} = 5$$

$$125 - 5 \times 3 = 110$$

$$\rightarrow x + \frac{1}{x} = \sqrt{\quad} \rightarrow x^3 + \frac{1}{x^3} = ?$$

$$x - \frac{1}{x} = \checkmark$$

$$x^2 + x = 5$$

$$x+3=t$$

$$x=t-3$$

$$x=t-3$$

$$t^2 - 6t + 9 + t - 3 = 5$$

$$\Rightarrow t^2 - 5t + 1 = 0$$

$$\Rightarrow t + \frac{1}{t} = 5$$

$$(x+3)^3 + \frac{1}{(x+3)^3} = ?$$

$$t^3 + \frac{1}{t^3}$$

240. If $x^2 + 4x - 4 = 0$, then $(x+5)^3 + \frac{1}{(x+5)^3} = ?$

यदि $x^2 + 4x - 4 = 0$ है, तो $(x+5)^3 + \frac{1}{(x+5)^3}$ का मान होगा :

a) 234

~~b) 198~~ $\rightarrow 4-4x$

c) 216

d) 110

$$(x+5) + \frac{1}{(x+5)} = \frac{x^2 + 10x + 25 + 1}{x+5} = \frac{6x + 30}{x+5} = 6$$

$$216 - 18 = 198$$

24). If $x^2 - 12x + 33 = 0$, then what is the value of $(x-4)^2 + \left[\frac{1}{(x-4)^2}\right]$?

यदि $x^2 - 12x + 33 = 0$ है, तो $(x-4)^2 + \left[\frac{1}{(x-4)^2}\right]$ का मान क्या है?

a) 16

b) ~~14~~
^{12x-33}

c) 18

d) 20

$$(x-4) + \frac{1}{(x-4)} = \frac{x^2 - 8x + 16 + 1}{x-4} = \frac{4x - 16}{x-4} = 4$$

$$16 - 2 = 14$$

242. If $x^2 + 2x = 4$, then $(x+3)^3 - \frac{1}{(x+3)^3} = ?$

यदि $x^2 + 2x = 4$ है, तो $(x+3)^3 - \frac{1}{(x+3)^3}$ का मान होगा :

- ~~a) 76~~ b) 64 c) 52 d) 36

$$(x+3) - \frac{1}{(x+3)} = \frac{x^3 + 6x^2 + 9 - 1}{x+3} = \frac{4x + 12}{x+3} = 4$$

$$4 \times 12 = 76$$

243. If $x^2 - 16x + 59 = 0$, then what is the value of $(x - 6)^2 + \frac{1}{(x-6)^2}$?

यदि $x^2 - 16x + 59 = 0$ है, तो $(x - 6)^2 + \frac{1}{(x-6)^2}$ का मान क्या है?

a) 14

b) 18

c) 16

d) 20

$$(x-6) + \frac{1}{(x-6)} = \frac{x^2 - 12x + 36 + 1}{x-6} = \frac{4x - 24}{x-6} \times$$

\downarrow

$$16+2=18$$

coaching center

Misc. $(x + \frac{1}{x})$

coaching center

244. If $\sqrt{x} + \frac{1}{\sqrt{x}} = 3$, $x > 0$, then the value of $x^2(x^2 - 47)$ is .

यदि $\sqrt{x} + \frac{1}{\sqrt{x}} = 3$, $x > 0$, है, तो $x^2(x^2 - 47)$ का मान होगा :

a) 0

b) 2

~~c) -1~~

d) 2

$$x + \frac{1}{x} = 3 - 2 = 1$$

$$x^2 + \frac{1}{x^2} = 47$$

$$\Rightarrow x^2 - 47 = -\frac{1}{x^2}$$

coaching center

$$x^4 + \frac{1}{x^4} = 47 + 2$$

$$x^2 + \frac{1}{x^2} = 7 + 2$$

$$x + \frac{1}{x} = 3$$

$$x - \frac{1}{x} = \sqrt{5}$$

$$5 = (3 + \sqrt{5} - 3)^2$$

$$x = \frac{3 + \sqrt{5}}{2}$$

245. If $x^4 + x^{-4} = 47, (x > 0)$
then the value of $(2x - 3)^2$ is:

अगर $x^4 + x^{-4} = 47, (x > 0)$
तो $(2x - 3)^2$ का मान है:

- a) 2
~~c) 5~~

- b) 3
d) 4

$$\begin{aligned} a+b &= 6 \\ a-b &= 2 \\ \text{Sum} \sum & \quad \oplus - \ominus \\ \hline & \quad \div \end{aligned}$$

$$(2x-3)^2 = 4x^2 - 12x + 9$$

$$\frac{x+1}{x} = 3$$

$$\Rightarrow x^2 + 1 = 3x$$

$$x^2 = \underline{3x-1}$$

$$\cancel{12x} - 4 - \cancel{12x} + 9 = 5$$

coaching center

246. If $x^4 + x^{-4} = 194$, ($x > 0$)
then the value of $(2x - 4)^2$
is:

अगर $x^4 + x^{-4} = 194$, ($x > 0$)
तो $(2x - 4)^2$ का मान है:

- a) 15 b) 20
~~c) 12~~ d) 16

$$x + \frac{1}{x} = 4$$

$$x - \frac{1}{x} = \sqrt{12}$$

$$x = \frac{4 + \sqrt{12}}{2}$$

$$(4 + \sqrt{12} - 4)^2 = 12$$

coaching center

247. If $x^2 - 9x + 1 = 0$ what is the value $x^8 - 6239x^4 + 1$?

यदि $x^2 - 9x + 1 = 0$ है, तो $x^8 - 6239x^4 + 1$ का मान क्या होगा ?

- a) 2 ~~b) 0~~
c) -1 d) 1

$$x + \frac{1}{x} = 9$$

$$x^2 + \frac{1}{x^2} = 79$$

$$\Rightarrow \left(x^4 + \frac{1}{x^4} = 6241 - 2 = 6239 \right) \times x^4$$

$$x^8 - 6239x^4 + 1 = 0$$

coaching center

248. If $x^2 - 8x + 1 = 0$, what is the value of $x^8 - 3842x^4 + 1$?

यदि $x^2 - 8x + 1 = 0$ है, तो $x^8 - 3842x^4 + 1$ का मान ज्ञात कीजिए।

- a) 1
~~b) 0~~
c) 2
c) -1

$$x + \frac{1}{x} = 8$$

$$x^2 + \frac{1}{x^2} = 62$$

$$\left(x^4 + \frac{1}{x^4} = 3844 - 2 = 3842 \right) \times x^4$$

$$x^8 - 3842x^4 + 1 = 0$$

coaching center

249. If $\frac{3(x^2+1)-7x}{3x} = 6$, $x \neq 0$, then the value of $\sqrt{x} + \frac{1}{\sqrt{x}}$ is:

यदि $\frac{3(x^2+1)-7x}{3x} = 6$, $x \neq 0$ है, तो $\sqrt{x} + \frac{1}{\sqrt{x}}$ का मान क्या होगा?

$$x^2 + \frac{1}{x^2} + 2 = 47 + 2$$

$$\left(x + \frac{1}{x}\right)^2 = 49$$

a) $\sqrt{\frac{25}{3}}$

b) $\sqrt{\frac{11}{3}}$

c) $\sqrt{\frac{35}{3}}$

d) ~~$\sqrt{\frac{31}{3}}$~~

$$x + \frac{1}{x} - \frac{7}{3} = 6$$

$$x + \frac{1}{x} + 2 = 6 + \frac{7}{3} = \frac{25}{3} + 2$$

$$\left(\sqrt{x}\right)^2 + \frac{1}{\left(\sqrt{x}\right)^2} + 2\sqrt{x} - \frac{1}{\sqrt{x}} = \frac{31}{3}$$

$$\left(\sqrt{x} + \frac{1}{\sqrt{x}}\right)^2 = \frac{31}{3}$$

$$\sqrt{x} + \frac{1}{\sqrt{x}} = \sqrt{\frac{31}{3}}$$

$$x = 1 + \sqrt{2}$$

$$\frac{1}{x} = \frac{1}{1+\sqrt{2}} = \frac{1-\sqrt{2}}{1-2} = \sqrt{2}-1$$

$$x + \frac{1}{x} = 2\sqrt{2} + 2$$

$$\left(x + \frac{1}{x} \right)^2 = \sqrt{2+2\sqrt{2}} \\ (1.414)$$

$$\begin{array}{r|rrr} 2 & \overline{4.8280} \\ \hline 41 & 82 \\ & 41 \\ \hline & 400 \\ & 400 \\ \hline & 0 \end{array}$$

250. If $x = 1 + \sqrt{2}$, then find the value of $\sqrt{x} + \frac{1}{\sqrt{x}}$.

यदि $x = 1 + \sqrt{2}$, तो $\sqrt{x} + \frac{1}{\sqrt{x}}$ का मान ज्ञात कीजिए।

a) 2.1014

~~b) 1.9876~~

~~b) 2.1973~~

~~c) 1.9996~~

$$\begin{array}{r} 2828 \\ +2 \\ \hline 4.828 \end{array}$$

$$\sqrt{2} = 1.414$$

$$\sqrt{3} = 1.732$$

$$\sqrt{5} = 2.236$$

coaching center

$$x + \frac{1}{x} = 47 + 2$$

$$\sqrt{x + \frac{1}{x}} = 7 + 2$$

$$x^{\frac{1}{4}} + \frac{1}{x^{\frac{1}{4}}} = 3$$

251. If $x^2 - 4x + 1 = 0$, then what is the value of $x^9 + x^7 - 194x^5 - 194x^3$?

यदि $x^2 - 4x + 1 = 0$ है, तो $x^9 + x^7 - 194x^5 - 194x^3$ का मान क्या है?

a) 4

$$\downarrow -x$$

$$x + \frac{1}{x} = 4$$

$$x^2 + \frac{1}{x^2} = 14$$

$$x^4 + \frac{1}{x^4} = 194$$

$$x^4 - 194 = -\frac{1}{x^4}$$

c) 1

d) -1

$$x^5(x^4 - 194) + x^3(x^4 - 194)$$

$$= x^5 \frac{x-1}{x^4} + x^3 \frac{x-1}{x^4}$$

$$= -x - \frac{1}{x}$$

$$= -(x + \frac{1}{x}) = -4$$

252. If $p + \frac{1}{p} = 112$ find $(p - 112)^{15} + \frac{1}{p^{15}}$.

यदि $p + \frac{1}{p} = 112$ है, $(p - 112)^{15} + \frac{1}{p^{15}}$ तो ज्ञात करो।

- a) 10 b) 0 c) 15 d) 1

$$p - 112 = -\frac{1}{p}$$

$$\left(\frac{-1}{p}\right)^{15} + \frac{1}{p^{15}}$$

$$= -\frac{1}{p^{15}} + \frac{1}{p^{15}} = 0$$

coaching center

253. If $x + \frac{2}{x} = 1$, then $\frac{x^2+x+2}{x^2(1-x)} = ?$

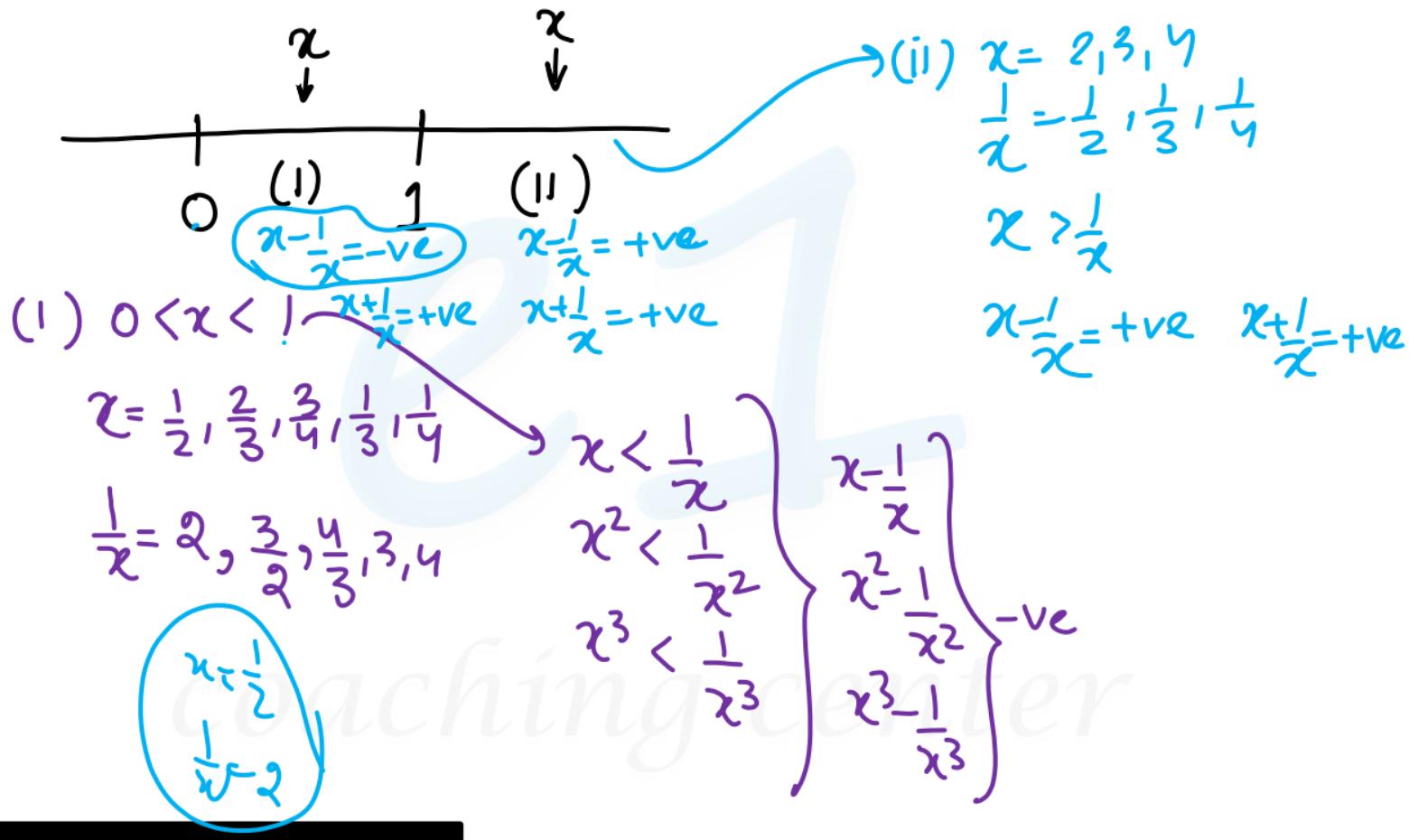
अगर $x + \frac{2}{x} = 1$ है तो $\frac{(x^2+x+2)/x}{(x^2(1-x))/x} = ?$

- a) 1 b) -1 c) 2 d) -2

$$\frac{2}{x} = 1-x$$

$$1 = \frac{2}{x(1-\frac{2}{x})} = \frac{\cancel{x} + \frac{2}{\cancel{x}} + 1}{\cancel{x}(1-\cancel{x})}$$

coaching center



$$x^2 - \frac{1}{x^2} = -21\sqrt{5}$$

$$\left[\begin{array}{l} x + \frac{1}{x} = 7 \\ x - \frac{1}{x} = -\sqrt{45} = -3\sqrt{5} \end{array} \right]$$

÷ x

254. If $x^2 - 7x + 1 = 0$, and $0 < x < 1$, what is the value of $x^2 - \frac{1}{x^2}$?

यदि $x^2 - 7x + 1 = 0$, और
 $0 < x < 1$, है, तो $x^2 - \frac{1}{x^2}$ का
मान क्या होगा?

- a) $21\sqrt{5}$ ~~b) $-21\sqrt{5}$~~
c) $28\sqrt{5}$ d) $-28\sqrt{5}$

coaching center

255. If $\left(x^2 + \frac{1}{x^2}\right) = 7$, and $0 < x < 1$, find
the value of $x^2 - \frac{1}{x^2}$. $x^n - \frac{1}{x^n} = -ve$

यदि $\left(x^2 + \frac{1}{x^2}\right) = 7$ और $0 < x < 1$
है, तो $x^2 - \frac{1}{x^2}$ का मान ज्ञात करें।

- a) $3\sqrt{5}$ b) $4\sqrt{3}$
c) $-4\sqrt{3}$ d) ~~$-3\sqrt{5}$~~

$$\begin{aligned} & -\sqrt{x^2 - 4} = -\sqrt{45} \\ & = -3\sqrt{5} \end{aligned}$$

coaching center

256. If $\left(x^2 + \frac{1}{x^2}\right) = 6$, and $0 < x < 1$,
what is the value of $x^4 - \frac{1}{x^4}$?

यदि $\left(x^2 + \frac{1}{x^2}\right) = 6$ और $0 < x < 1$, है, तो $x^4 - \frac{1}{x^4}$ का मान क्या होगा?

$$\left(x^2 + \frac{1}{x^2}\right)\left(x^2 - \frac{1}{x^2}\right)$$

$$= 6 \times -4\sqrt{2}$$

- a) $24\sqrt{2}$
c) $-12\sqrt{10}$

- ~~b) $-24\sqrt{2}$~~
d) $12\sqrt{10}$

$$x^2 - \frac{1}{x^2} = \sqrt{36 - 4} = -4\sqrt{2}$$

coaching center